

Magnetism (FM, AFM, FSM)

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- In localized systems (e.g. some rare earth) the magnetism is mainly governed by the atom (Hund's rule)
- In itinerant (delocalized) systems (many transition metals) magnetism comes from partial occupation of states, which differ between spin-up and spin-down.
- Boarderline cases (some f-electron systems) details of the structure (e.g. lattice spacing) determine whether or not some electrons are localized or itinerant.

Ferro-, antiferro-, or ferri-magnetic

• Ferromagnetic (FM) (e.g. bcc Fe)

$$\oint \oint \oint \oint \oint \oint \oint \oint \oint M > 0$$

Antiferromagnetic (AFM) (e.g. Cr)

Ferrimagnetic cases

the moments at different atoms are antiparallel but of different magnitude

Non-collinear magnetism (NCM)

the magnetic moments are not ligned up parallel.

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Experimental facts:

	$\sigma[m emu/g]$	$\sigma\left[\mu_{ m B} ight]$	$T_{ m c}[{ m K}]$	ρ at 298K [g/cm ³]
Fe (bcc)	221.7	2.22	1044	7.875
Co~(fcc)	166.1	1.75	1388	8.793
Co~(hcp)	163.1	1.72	1360	8.804
Ni (fcc)	58.6	0.62	627	8.912
			1	
		Curie temperature		



- 1. The carriers of magnetism are the unsaturated spins in the d-band.
- 2. Effects of exchange are treated with a molecular field term.
- 3. One must conform to Fermi statistics.

Stoner, 1936





In a

- non magnetic (NM) case
 - $\mathbf{N}_{\uparrow} = \mathbf{N}_{\downarrow}$ (spin-up and spin-down)
- ferromagnetic (FM) case

 $\mathbb{N}_{\uparrow} > \mathbb{N}_{\downarrow}$ (majority and minority spin) the moments at all sites are parallel (collinear)

- the (spin) magnetic moment m
 - $\bullet m = N_{\uparrow} N_{\downarrow}$
 - its orientation with respect to the crystal axes is only defined by spin orbit coupling.
- there can also be an orbital moment

it is often suppressed in 3d transition metals

$$\chi = rac{\chi_{\mathrm{P}}}{1 - 2\mu_{\mathrm{B}}^2 I_{\mathrm{s}} \mathcal{N}\left(\varepsilon_{\mathrm{F}}\right)} = \chi_{\mathrm{P}} S$$

Exchange splitting



 $2\mu_{\rm B}^2 I_{\rm s} \mathcal{N}\left(\varepsilon_{\rm F}\right) > 1$

Stoner criterion





- The existence of ferromagnetism (FM) is governed by the
- Stoner criterion

 $I.N(E_F) > 1$

- N(E_F)DOS at E_F(of NM case)IStoner parameter~ independent of structure
- Ferromagnetism appears when the gain in exchange energy is larger than the loss in kinetic energy



P.James, O.Eriksson, B.Johansson, I.A.Abrikosov, Phys.Rev.B **58**, ... (1998)



$\rm E_{\rm F}$ at high DOS















V. Heine: "metals are systems with unsaturated covalent bonds"









e.g. Fe-Co alloys

Wigner delay times



Spin projected DOS of Fe-Co alloys





 The alloy is represented by ordered structures

- Fe₃Co and FeCo₃ (Heusler)
- FeCo Zintl or CsCl
- *Fe, Co bcc*



oCo







Itinerant or localized?





Magnetization density in FeCo



- Magnetization density difference between
 - Majoity spin
 - Minority spin

$m(r) = \rho^{\dagger}(r) - \rho^{\downarrow}(r)$

Localized around

- Fe and Co
- slightly negative between the atoms
- Itinerant electrons

K.Schwarz, P.Mohn, P.Blaha, J.Kübler, *Electronic and magnetic structure of bcc Fe-Co alloys from band theory,*J.Phys.F:Met.Phys. **14**, 2659 (1984)























Covalent magnetism, FeCo:







Cr has AFM bcc structure





 There is a symmetry it is enough to do the spin-up calculation spin-down can be copied

$$Cr_1^{\downarrow} = Cr_2^{\uparrow}$$

 $Cr_2^{\downarrow} = Cr_1^{\uparrow}$





- Al-silicate
- corner shared
 - SiO₄ tetrahedra
 - AlO₄ tetrahedra
- β cage
- Al / Si ratio 1
- alternating
- ordered (cubic)
- 3 e⁻ per cage







- Si-Al zeolite (sodalite)
 - Formed by corner-shared SiO₄ and AlO₄ tetrahedra
- Charge compensated by doping with
 - 4 Na⁺
 - one e⁻ (color center)
- antiferromagnetic (AFM) order of e⁻



Energy (relative stability)







AFM order between color centers (e⁻)

Spin density ρ^{\uparrow} - ρ^{\downarrow}





G.K.H. Madsen, Bo B. Iversen, P. Blaha, K. Schwarz, Phys. Rev. B 64, 195102 (2001)





e.g. Fe-Ni

 Such systems essentially show no thermal expansion around room temperature







- The thermal expansion of the Eifel tower
- Measured with a rigid Fe-Ni INVAR wire
- The length of the tower correlates with the temperature
- Fe₆₅Ni₃₅ alloy has vanishing thermal expansion around room temperature





What is magnetostriction?

Magnetostriction ω_{s0} is the difference in volume between the volume in the magnetic ground state and the volume in a hypothetical non-magnetic state.

Above the Curie temperature the magnetic contribution ω_m vanishes.







"classical" Fe-Ni Invar





A.R.Williams, V.L.Moruzzi, G.D.Gelatt Jr., J.Kübler, K.Schwarz, *Aspects of transition metal magnetism*,J.Appl.Phys. **53**, 2019 (1982)







- Energy surface at T=0 (DFT)
 - as a function of volume and moment
 - using fixed spin moment (FSM) calculations
- Finite temperature
 - Spin and volume fluctuations
 - Ginzburg-Landau model

$$H = V^{-1} \int d^3r \left(E(M + \underline{m(r)}), V + \underline{v(r)} \right)$$
$$+ \frac{C}{2} \sum_{ij} \left(\nabla_j \underline{m}_i \right)^2 + \frac{D}{2} (\nabla v(r))^2 \right)$$







fixed spin moment (FSM)
 e.g. Fe-Ni alloy

 allows to explore energy surface E(V,M) as function of
 volume
 magnetic moment





- There are systems (e.g. like fcc Fe or fcc Co), for which the magnetization shows a hysteresis, when a magnetic field is applied (at a volume V).
- The volume of the unit cell defines the Wigner-Seitz radius rws

$$V = \frac{4 \pi r_{WS}^3}{3}$$

- The hysteresis causes numerical difficulties, since there are several solutions (in the present case 3 for a certain field H).
- In order to solve this problem the FSM method was invented

Hysteresis











- Physical situation:
 - One applies a field H and obtains M
 - but this functions can be multivalued

- Computational trick (unphysical):
 - One interchanges the dependent and independent variable
 - this function is single valued (unique)
 - i.e. one chooses M and calculates H afterwards











A.R.Williams, V.L.Moruzzi, J.Kübler, K.Schwarz, Bull.Am.Phys.Soc. **29**, 278 (1984)

K.Schwarz, P.Mohn J.Phys.F **14**, L129 (1984)

P.H.Dederichs, S.Blügel, R.Zoller, H.Akai, Phys. Rev, Lett. **53**,2512 (1984)





GMR (Giant Magneto Resistance)

half-metallic systems e.g. CrO₂

important for spintronics




Once upon a time, in the early 1980's ...



Peter Grünberg



$$GMR = \frac{R_{AP} - R_P}{R_P}$$

19% for trilayers @RT80% for multilayers @ RT

GMR is much larger than the anisotropic magnetoresistance (AMR)



1988: ... simultaneously, but independent ...





"Does the electrical resistance depend on the magnetization alignment?"





Albert Fert



Peter Grünberg

9 October 2007







The Nobel Prize in Physics 2007



This year's Nobel Prize in Physics is awarded to Albert Fert and Peter Grünberg for their discovery of Giant Magnetoresistance. Applications of this phenomenon have revolutionized

techniques for retrieving data from hard disks.

Scientific Background on the Nobel Prize in Physics 2007

The Discovery of Giant Magnetoresistance

compiled by the Class for Physics of the Royal Swedish Academy of Sciences

4. Half-metals

Since magnetoresistance deals with electrical conductivity it is obvious that it is the behaviour of the electrons at the Femi surface (defined by the Fermi energy) which is of primary interest. The more spin-polarized the density of states (DOS) at the Fermi energy, i.e., the more N_{\uparrow} (E_F) deviates from N_{\downarrow} (E_F), the more pronounced one expects the efficiency of the magnetoelectronic effects to be. In this respect a very interesting class of materials consists of what are called half-metals, a concept introduced by de Groot and co-workers (23). Such a property was then predicted theoretically for CrO_2 by Schwarz in 1986 (24). The name half-metal originates from the particular feature that the spin down band is metallic while the spin up band is an insulator.

24. K. Schwarz, "CrO₂ predicted as a half-metallic ferromagnet", J. Phys. F, 16, L211 (1986).

http://www.kva.se/

Scientific background



CrO₂ (rutile structure)





important for spintronics



- The DOS features of CrO₂ are qualitatively like
 - TiO₂ (for spin-down)



K.Schwarz,

CrO₂ predicted as a

half-metallic ferromagnet,

J.Phys.F:Met.Phys. 16, L211 (1986)

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6

7

8

all three compound crystallize in the rutile structure







CrO₂ (rutile structure)







1 2	1 1.008 3 6.941 11	2 4 9.012 12		6 C 12.01	Sym	nic nu bol nic we		Metal Semimetal Nonmetal					13 5 10.81 13	14 6 12.01 14	7 7 14.01 15	16 8 16.00 16	9 F 19.00 17	18 2 He 4.003 10 Ne 20.18 18
3	Na 22.99	Mg	3	4	5	6	7	8	9	10	11	12	Al 26.98	Si	P 30.97	S	C1 35.45	
	<u>22.99</u> 19	24.31	21	22	23	24	25	26	27	28	29	30	<u>20.90</u> 31	28.09 32	30.97	<u>32.07</u> 34	35	39.95 36
4	K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se	Br	Kr
	39.10	40.08	44.96	47.88	50.94	52.00	54.94	55.85	58.93	58.69	63.55	65.39	69.72	72.61	74.92	78.96	79.90	83.80
_	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54
- 5	Rb	Sr	Y	Zr	Nb	Mo	TC	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te	Ι	Xe
	85.47	87.62	88.91	91.22	92.91	95.94	98.91	101.1	102.9	106.4	107.9	112.4	114.8	118.7	121.8	127.6	126.9	131.3
	55	56	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86
6	Cs	Ba	Lu	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	T1	Pb	Bi	Po	At	Rn
	132.9	137.3	175.0	178.5	180.9	183.8	186.2	190.2	192.2	195.1	197.0	200.6	204.4	207.2	209.0	209.0	210.0	222.0
-	87	88	103	104	105	106	107	108	109	110	111	112	113	114	115	116	117	118
7	Fr	Ra	Lr	Rf	Db	Sg	Bh	Hs	Mt	Uun		Uub	Uut.		Uup	Uuh	Uus.	Uuo
	223.0	226.0	262.1	261.1	262.1	263.1	264.1	265.1	268	269	272	277		289 🗍	_	289		293
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Magnetic structure of uranium dioxide UO₂



- R.Laskowski
- G.K.H.Madsen
- P.Blaha
- K.Schwarz







- topics
 - non-collinear magnetism
 - spin-orbit coupling
 - LDA+U (correlation of U-5f electrons)
 - Structure relaxations
 - electric field gradient (EFG)



R.Laskowski, G.K.H.Madsen, P.Blaha, K.Schwarz: *Magnetic structure and electric-field gradients of uranium dioxide: An ab initio study* Phys.Rev.B **69**, 140408-1-4 (2004)









non-collinear magnetism in UO₂











- Magnetisation direction
 perpenticular at the two U sites (arrows)
- Magnetisation density (color)







Wien2k can only handle collinear or non-magnetic cases







- runsp_lapw script (unconstrained magnetic calc.)
 - runs lapw1/2 for both spins independently
 - case.scf contains extra information:
 - grep :MMT case.scf (for total moment)
 - grep :MMI case.scf (for atomic moments)
 - grep : HFF case.scf (for hyperfine fields)





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 - grep :MMT case.scf (for total moment)
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 - grep : HFF case.scf (for hyperfine fields)
- runfsm_lapw -m value (constrained moment calc.)
 - for difficult to converge magnetic cases or simply to constrain a moment (→ 2 Fermi-energies → external magnetic field)
- runafm_lapw (anti-ferromagnetic calculation)
 - calculates only spin-up, uses symmetry to generate spin-dn





- runsp_lapw script (unconstrained magnetic calc.)
- runfsm_lapw -m value (constrained moment calc.)
- runafm_lapw (anti-ferromagnetic calculation)
 - spin-orbit coupling can be included in second variational step
 - never mix polarized and non-polarized calculations in one case directory !!!



Thank you for your attention



